

tropical algebra

tropical algebra represents a fascinating branch of mathematics that integrates algebraic concepts with tropical geometry. This area of study has gained significant traction in recent years, especially due to its applications in various fields such as combinatorial optimization, algebraic geometry, and even mathematical biology. This article will explore the foundations of tropical algebra, its key principles, applications, and the interplay between tropical algebra and other mathematical disciplines. Furthermore, we will provide a comprehensive understanding of the core concepts, making this a valuable resource for students, researchers, and anyone interested in this innovative field.

- Introduction to Tropical Algebra
- Key Concepts in Tropical Algebra
- Applications of Tropical Algebra
- Tropical Algebra and Combinatorics
- The Relationship Between Tropical Algebra and Algebraic Geometry
- Future Directions in Tropical Algebra
- Conclusion

Introduction to Tropical Algebra

Tropical algebra is fundamentally different from classical algebra, as it operates under a distinct set of

rules. In tropical algebra, the operations of addition and multiplication are redefined; specifically, addition is replaced by taking the minimum (or maximum) of two values, and multiplication is performed through standard addition. This unconventional approach allows for a unique framework that can simplify many problems in algebraic geometry and combinatorial optimization. The beauty of tropical algebra lies in its ability to transform complex algebraic structures into more manageable forms, thus aiding in the analysis of various mathematical problems.

Key Concepts in Tropical Algebra

To fully grasp tropical algebra, it is essential to understand its foundational concepts. The key elements include tropical semirings, tropical polynomials, and tropical varieties.

Tropical Semirings

A tropical semiring is an algebraic structure consisting of a set equipped with two operations: tropical addition and tropical multiplication. The tropical addition of two elements (a) and (b) is defined as $(\min(a, b))$, while tropical multiplication is defined as $(a + b)$. In this context, the properties of semirings, such as associativity and commutativity, still hold, making tropical semirings a robust framework for mathematical exploration.

Tropical Polynomials

Tropical polynomials are another crucial aspect of tropical algebra. A tropical polynomial is a finite sum of monomials with coefficients from a tropical semiring. The form of a tropical polynomial can be expressed as:

$$P(x) = \min(a_1 + x^{k_1}, a_2 + x^{k_2}, \dots, a_n + x^{k_n})$$

where (a_i) are the coefficients and (k_i) are the respective degrees. Analyzing tropical polynomials is essential for solving tropical equations and studying tropical varieties.

Tropical Varieties

Tropical varieties can be understood as the geometric manifestations of tropical polynomials. They provide a way to visualize the solutions of tropical equations. The concept of tropical varieties has significant implications in algebraic geometry, as it allows mathematicians to study geometric properties using a simplified algebraic framework. Notably, tropical varieties can be seen as piecewise-linear objects, which makes them easier to analyze than their classical counterparts.

Applications of Tropical Algebra

Tropical algebra has a wide range of applications across various fields, showcasing its versatility and power. Some of the most prominent applications include optimization, computational biology, and network theory.

Optimization

One of the most significant applications of tropical algebra is in combinatorial optimization. Many optimization problems can be formulated in terms of tropical algebra, particularly those involving shortest paths and maximum flows. The tropical framework simplifies the complexity of these problems, enabling more efficient algorithms to be developed.

Computational Biology

Tropical algebra also finds applications in computational biology, particularly in the analysis of phylogenetic trees. By using tropical methods, researchers can model the evolutionary relationships between species more effectively. The tropical approach provides a new lens through which to view biological data, facilitating the extraction of meaningful insights.

Network Theory

In network theory, tropical algebra is used to analyze and optimize network flows. The ability to model complex systems using tropical mathematics allows for improved efficiency in network design and resource allocation. This application is particularly valuable in fields such as telecommunications and transportation.

Tropical Algebra and Combinatorics

The intersection of tropical algebra and combinatorics has led to significant advancements in both fields. The combinatorial structures that arise from tropical algebra can provide insights into various mathematical problems.

Tropical Polytopes

Tropical polytopes are a combinatorial counterpart to classical polytopes. They can be defined as the convex hull of points in tropical space and have applications in enumerative combinatorics. The study of tropical polytopes has revealed deep connections between algebraic geometry and combinatorial optimization.

Invariants and Their Applications

Invariants in tropical algebra, such as the tropical rank of matrices, can be utilized to study linear transformations and their properties. These invariants play a crucial role in understanding the underlying structure of various mathematical objects, bridging the gap between algebraic and combinatorial perspectives.

The Relationship Between Tropical Algebra and Algebraic Geometry

The relationship between tropical algebra and algebraic geometry is profound and has led to a deeper understanding of both areas. Tropical algebra serves as a powerful tool for studying the properties of algebraic varieties.

Tropicalization

Tropicalization is the process of converting classical algebraic varieties into their tropical counterparts. This transformation allows mathematicians to leverage the piecewise-linear structure of tropical varieties to gain insights into the properties of classical varieties. The tropicalization process has become a crucial method for solving problems in algebraic geometry.

Applications in Intersection Theory

In intersection theory, tropical algebra provides techniques for analyzing the intersections of algebraic varieties. By studying the tropical intersections, mathematicians can derive information about classical intersections, leading to new results and conjectures in the field.

Future Directions in Tropical Algebra

The future of tropical algebra is promising, with ongoing research uncovering new applications and connections to other mathematical fields. As the discipline continues to evolve, several areas show particular potential for growth.

Interdisciplinary Research

Interdisciplinary research that combines tropical algebra with fields such as computer science, physics, and economics is likely to yield exciting developments. The adaptability of tropical algebra makes it a suitable framework for tackling complex problems across various domains.

Advancements in Computational Methods

As computational methods improve, the ability to apply tropical algebra to larger and more complex systems will enhance its applications in optimization and data analysis. Developing efficient algorithms will be critical in expanding the scope of problems that can be addressed using tropical methods.

Conclusion

Tropical algebra is a rich and evolving field that bridges several areas of mathematics. By reinterpreting classical algebra through the lens of tropical geometry, researchers can simplify complex problems and uncover new relationships between different mathematical concepts. The applications of tropical algebra are vast, spanning optimization, biology, and combinatorics, and its interplay with algebraic geometry continues to reveal deeper insights into the nature of mathematical structures. As the field progresses, the potential for future discoveries remains immense, promising to influence both theoretical and applied mathematics in profound ways.

Q: What is tropical algebra?

A: Tropical algebra is a mathematical framework that redefines addition and multiplication, using the minimum and maximum operations respectively. It provides a unique perspective on algebraic structures and has applications in various fields such as optimization and algebraic geometry.

Q: How does tropical algebra differ from classical algebra?

A: The main difference lies in the operations used; tropical algebra uses tropical addition (minimum) and tropical multiplication (addition), as opposed to the traditional operations in classical algebra. This leads to different properties and structures within the algebraic framework.

Q: What are tropical polynomials?

A: Tropical polynomials are expressions formed from tropical semirings, where the operations involve taking the minimum and adding coefficients. They play a crucial role in defining tropical varieties and solving tropical equations.

Q: What are the main applications of tropical algebra?

A: Tropical algebra has applications in optimization problems, computational biology, and network theory. It simplifies complex problems, making it easier to analyze and derive solutions in these fields.

Q: What is the relationship between tropical algebra and algebraic geometry?

A: Tropical algebra serves as a tool for studying algebraic geometry by transforming classical algebraic varieties into tropical varieties. This connection allows for the analysis of geometric properties through tropical methods.

Q: How does tropicalization work?

A: Tropicalization is the process of converting classical algebraic structures into their tropical forms. This transformation simplifies the analysis of algebraic varieties, allowing mathematicians to study them using piecewise-linear techniques.

Q: What are tropical varieties?

A: Tropical varieties are geometric structures that arise from tropical polynomials. They represent the solutions to tropical equations and have a piecewise-linear nature, making them more manageable than classical varieties.

Q: Why is tropical algebra important in optimization?

A: Tropical algebra simplifies many combinatorial optimization problems, such as shortest paths and maximum flows, allowing for more efficient algorithms and solutions in network design and resource allocation.

Q: What future directions are being explored in tropical algebra?

A: Future directions include interdisciplinary research that integrates tropical algebra with other fields, as well as advancements in computational methods that will expand its applications to more complex systems and problems.

Tropical Algebra

Find other PDF articles:

<http://www.speargroupllc.com/gacor1-22/Book?trackid=BRQ26-6562&title=olympia-of-infidelity-characters.pdf>

tropical algebra: Introduction to Tropical Geometry Diane Maclagan, Bernd Sturmfels, 2021-12-13 Tropical geometry is a combinatorial shadow of algebraic geometry, offering new polyhedral tools to compute invariants of algebraic varieties. It is based on tropical algebra, where the sum of two numbers is their minimum and the product is their sum. This turns polynomials into piecewise-linear functions, and their zero sets into polyhedral complexes. These tropical varieties retain a surprising amount of information about their classical counterparts. Tropical geometry is a young subject that has undergone a rapid development since the beginning of the 21st century. While establishing itself as an area in its own right, deep connections have been made to many branches of pure and applied mathematics. This book offers a self-contained introduction to tropical

geometry, suitable as a course text for beginning graduate students. Proofs are provided for the main results, such as the Fundamental Theorem and the Structure Theorem. Numerous examples and explicit computations illustrate the main concepts. Each of the six chapters concludes with problems that will help the readers to practice their tropical skills, and to gain access to the research literature. This wonderful book will appeal to students and researchers of all stripes: it begins at an undergraduate level and ends with deep connections to toric varieties, compactifications, and degenerations. In between, the authors provide the first complete proofs in book form of many fundamental results in the subject. The pages are sprinkled with illuminating examples, applications, and exercises, and the writing is lucid and meticulous throughout. It is that rare kind of book which will be used equally as an introductory text by students and as a reference for experts. —Matt Baker, Georgia Institute of Technology

Tropical geometry is an exciting new field, which requires tools from various parts of mathematics and has connections with many areas. A short definition is given by Maclagan and Sturmfels: “Tropical geometry is a marriage between algebraic and polyhedral geometry”. This wonderful book is a pleasant and rewarding journey through different landscapes, inviting the readers from a day at a beach to the hills of modern algebraic geometry. The authors present building blocks, examples and exercises as well as recent results in tropical geometry, with ingredients from algebra, combinatorics, symbolic computation, polyhedral geometry and algebraic geometry. The volume will appeal both to beginning graduate students willing to enter the field and to researchers, including experts. —Alicia Dickenstein, University of Buenos Aires, Argentina

tropical algebra: Introduction to Tropical Geometry Diane Maclagan, 2015 Cover -- Title page -- Copyright page -- Dedication -- Contents -- Preface -- Chapter 1. Tropical islands -- Chapter 2. Building blocks -- Chapter 3. Tropical varieties -- Chapter 4. Tropical rain forest -- Chapter 5. Tropical garden -- Chapter 6. Toric connections -- Bibliography -- Index -- Back Cover

tropical algebra: Tropical Algebraic Geometry Il'ia Vladimirovich Itenberg, Grigory Mikhalkin, Eugenio Shustin, 2007 Tropical geometry is algebraic geometry over the semifield of tropical numbers, i.e., the real numbers and negative infinity enhanced with the $(\max, +)$ -arithmetic. Geometrically, tropical varieties are much simpler than their classical counterparts. Yet they carry information about complex and real varieties. These notes present an introduction to tropical geometry and contain some applications of this rapidly developing and attractive subject. It consists of three chapters which complete each other and give a possibility for non-specialists to make the first steps in the subject which is not yet well represented in the literature. The intended audience is graduate, post-graduate, and Ph.D. students as well as established researchers in mathematics.

tropical algebra: Tropical and Idempotent Mathematics Grigoriĭ Lazarevich Litvinov, S. N. Sergeev, 2009 This volume is a collection of papers from the International Conference on Tropical and Idempotent Mathematics, held in Moscow, Russia in August 2007. This is a relatively new branch of mathematical sciences that has been rapidly developing and gaining popularity over the last decade. Tropical mathematics can be viewed as a result of the Maslov dequantization applied to 'traditional' mathematics over fields. Importantly, applications in econophysics and statistical mechanics lead to an explanation of the nature of financial crises. Another original application provides an analysis of instabilities in electrical power networks. Idempotent analysis, tropical algebra, and tropical geometry are the building blocks of the subject. Contributions to idempotent analysis are focused on the Hamilton-Jacobi semigroup, the max-plus finite element method, and on the representations of eigenfunctions of idempotent linear operators. Tropical algebras, consisting of plurisubharmonic functions and their germs, are examined. The volume also contains important surveys and research papers on tropical linear algebra and tropical convex geometry.

tropical algebra: Essentials of Tropical Combinatorics Michael Joswig, 2021-12-08 The goal of this book is to explain, at the graduate student level, connections between tropical geometry and optimization. Building bridges between these two subject areas is fruitful in two ways. Through tropical geometry optimization algorithms become applicable to questions in algebraic geometry.

Conversely, looking at topics in optimization through the tropical geometry lens adds an additional layer of structure. The author covers contemporary research topics that are relevant for applications such as phylogenetics, neural networks, combinatorial auctions, game theory, and computational complexity. This self-contained book grew out of several courses given at Technische Universität Berlin and elsewhere, and the main prerequisite for the reader is a basic knowledge in polytope theory. It contains a good number of exercises, many examples, beautiful figures, as well as explicit tools for computations using `polymake`.

tropical algebra: Tropical and Idempotent Mathematics and Applications Grigoriĭ Lazarevich Litvinov, S. N. Sergeev, 2014 This volume contains the proceedings of the International Workshop on Tropical and Idempotent Mathematics, held at the Independent University of Moscow, Russia, from August 26-31, 2012. The main purpose of the conference was to bring together and unite researchers and specialists in various areas of tropical and idempotent mathematics and applications. This volume contains articles on algebraic foundations of tropical mathematics as well as articles on applications of tropical mathematics in various fields as diverse as economics, electroenergetic networks, chemical reactions, representation theory, and foundations of classical thermodynamics. This volume is intended for graduate students and researchers interested in tropical and idempotent mathematics or in their applications in other areas of mathematics and in technical sciences.

tropical algebra: Algebraic and Combinatorial Aspects of Tropical Geometry Erwan Brugalle, Maria Angelica Cueto, Alicia Dickenstein, Eva-Maria Feichtner, Ilia Itenberg, 2013-05-23 This volume contains the proceedings of the CIEM workshop on Tropical Geometry, held December 12-16, 2011, at the International Centre for Mathematical Meetings (CIEM), Castro Urdiales, Spain. Tropical geometry is a new and rapidly developing field of mat

tropical algebra: Computer Algebra in Scientific Computing Vladimir P. Gerdt, Wolfram Koepf, Ernst W. Mayr, Evgenii V. Vorozhtsov, 2013-08-15 This book constitutes the proceedings of the 14th International Workshop on Computer Algebra in Scientific Computing, CASC 2013, held in Berlin, Germany, in September 2013. The 33 full papers presented were carefully reviewed and selected for inclusion in this book. The papers address issues such as polynomial algebra; the solution of tropical linear systems and tropical polynomial systems; the theory of matrices; the use of computer algebra for the investigation of various mathematical and applied topics related to ordinary differential equations (ODEs); applications of symbolic computations for solving partial differential equations (PDEs) in mathematical physics; problems arising at the application of computer algebra methods for finding infinitesimal symmetries; applications of symbolic and symbolic-numeric algorithms in mechanics and physics; automatic differentiation; the application of the CAS Mathematica for the simulation of quantum error correction in quantum computing; the application of the CAS GAP for the enumeration of Schur rings over the group A_5 ; constructive computation of zero separation bounds for arithmetic expressions; the parallel implementation of fast Fourier transforms with the aid of the Spiral library generation system; the use of object-oriented languages such as Java or Scala for implementation of categories as type classes; a survey of industrial applications of approximate computer algebra.

tropical algebra: Tropical Geometry and Integrable Systems Chris Athorne, Diane Maclagan, Ian Strachan, 2012 This volume contains the proceedings of the conference on tropical geometry and integrable systems, held July 3-8, 2011, at the University of Glasgow, United Kingdom. One of the aims of this conference was to bring together researchers in the field of tropical geometry and its applications, from apparently disparate ends of the spectrum, to foster a mutual understanding and establish a common language which will encourage further developments of the area. This aim is reflected in these articles, which cover areas from automata, through cluster algebras, to enumerative geometry. In addition, two survey articles are included which introduce ideas from researchers on one end of this spectrum to researchers on the other. This book is intended for graduate students and researchers interested in tropical geometry and integrable systems and the developing links between these two areas.

tropical algebra: Nonarchimedean and Tropical Geometry Matthew Baker, Sam Payne, 2016-08-18 This volume grew out of two Simons Symposia on Nonarchimedean and tropical geometry which took place on the island of St. John in April 2013 and in Puerto Rico in February 2015. Each meeting gathered a small group of experts working near the interface between tropical geometry and nonarchimedean analytic spaces for a series of inspiring and provocative lectures on cutting edge research, interspersed with lively discussions and collaborative work in small groups. The articles collected here, which include high-level surveys as well as original research, mirror the main themes of the two Symposia. Topics covered in this volume include: Differential forms and currents, and solutions of Monge-Ampere type differential equations on Berkovich spaces and their skeletons; The homotopy types of nonarchimedean analytifications; The existence of faithful tropicalizations which encode the topology and geometry of analytifications; Relations between nonarchimedean analytic spaces and algebraic geometry, including logarithmic schemes, birational geometry, and the geometry of algebraic curves; Extended notions of tropical varieties which relate to Huber's theory of adic spaces analogously to the way that usual tropical varieties relate to Berkovich spaces; and Relations between nonarchimedean geometry and combinatorics, including deep and fascinating connections between matroid theory, tropical geometry, and Hodge theory.

tropical algebra: Algorithmic and Experimental Methods in Algebra, Geometry, and Number Theory Gebhard Böckle, Wolfram Decker, Gunter Malle, 2018-03-22 This book presents state-of-the-art research and survey articles that highlight work done within the Priority Program SPP 1489 "Algorithmic and Experimental Methods in Algebra, Geometry and Number Theory", which was established and generously supported by the German Research Foundation (DFG) from 2010 to 2016. The goal of the program was to substantially advance algorithmic and experimental methods in the aforementioned disciplines, to combine the different methods where necessary, and to apply them to central questions in theory and practice. Of particular concern was the further development of freely available open source computer algebra systems and their interaction in order to create powerful new computational tools that transcend the boundaries of the individual disciplines involved. The book covers a broad range of topics addressing the design and theoretical foundations, implementation and the successful application of algebraic algorithms in order to solve mathematical research problems. It offers a valuable resource for all researchers, from graduate students through established experts, who are interested in the computational aspects of algebra, geometry, and/or number theory.

tropical algebra: Tropical Algebraic Geometry Ilia Itenberg, Grigory Mikhalkin, Eugenio I. Shustin, 2009-09-03 These notes present a polished introduction to tropical geometry and contain some applications of this rapidly developing and attractive subject. It consists of three chapters which complete each other and give a possibility for non-specialists to make the first steps in the subject which is not yet well represented in the literature. The notes are based on a seminar at the Mathematical Research Center in Oberwolfach in October 2004. The intended audience is graduate, post-graduate, and Ph.D. students as well as established researchers in mathematics.

tropical algebra: Algebraic Statistics for Computational Biology L. Pachter, B. Sturmfels, 2005-08-22 This book, first published in 2005, offers an introduction to the application of algebraic statistics to computational biology.

tropical algebra: Recent Developments in Algebra and Analysis Ho-Hon Leung, R. Sivaraj, Firuz Kamalov, 2024-02-22 This volume collects the proceedings of the International Conference on Recent Developments in Mathematics (ICRDM), held at Canadian University Dubai, UAE, in August 2022. It is the first of two volumes, this first volume focuses on recent advances in algebra and analysis, and the second volume covers more applied topics. Each chapter identifies existing challenges in these theoretical areas, and highlights the importance of establishing new theorems and algorithms to address them. Recent Developments in Algebra and Analysis will appeal to a range of postgraduate students and researchers who are interested in exploring more on these areas and play an integral role in modern science.

tropical algebra: Tropical Circuit Complexity Stasys Jukna, 2023-11-06 This book presents an

enticing introduction to tropical circuits and their use as a rigorous mathematical model for dynamic programming (DP), which is one of the most fundamental algorithmic paradigms for solving combinatorial, discrete optimization problems. In DP, an optimization problem is broken up into smaller subproblems that are solved recursively. Many classical DP algorithms are pure in that they only use the basic (min,+) or (max,+) operations in their recursion equations. In tropical circuits, these operations are used as gates. Thanks to the rigorous combinatorial nature of tropical circuits, elements from the Boolean and arithmetic circuit complexity can be used to obtain lower bounds for tropical circuits, which play a crucial role in understanding the limitations and capabilities of these computational models. This book aims to offer a toolbox for proving lower bounds on the size of tropical circuits. In this work, the reader will find lower-bound ideas and methods that have emerged in the last few years, with detailed proofs. Largely self-contained, this book is meant to be approachable by graduate students in mathematics and computer science with a special interest in circuit complexity.

tropical algebra: *Symmetries in Algebra and Number Theory (SANT)* Ina Kersten, Ralf Meyer, 2009 4e de couverture : These proceedings contain most of the contributions to the Göttingen-Jerusalem Conference 2008 on Symmetries in Algebra and Number Theory including three addresses given at the conference opening, and two contributions to the Satellite Conference On the Legacy of Hermann Weyl. The contributions are survey articles or report on recent work by the authors, for example new results on the famous Leopoldt conjecture.

tropical algebra: **Tropical and Non-Archimedean Geometry** Omid Amini, Matthew Baker, Xander Faber, 2014-12-26 Over the past decade, it has become apparent that tropical geometry and non-Archimedean geometry should be studied in tandem; each subject has a great deal to say about the other. This volume is a collection of articles dedicated to one or both of these disciplines. Some of the articles are based, at least in part, on the authors' lectures at the 2011 Bellairs Workshop in Number Theory, held from May 6-13, 2011, at the Bellairs Research Institute, Holetown, Barbados. Lecture topics covered in this volume include polyhedral structures on tropical varieties, the structure theory of non-Archimedean curves (algebraic, analytic, tropical, and formal), uniformisation theory for non-Archimedean curves and abelian varieties, and applications to Diophantine geometry. Additional articles selected for inclusion in this volume represent other facets of current research and illuminate connections between tropical geometry, non-Archimedean geometry, toric geometry, algebraic graph theory, and algorithmic aspects of systems of polynomial equations.

tropical algebra: *Proceedings of Third International Conference on Advanced Computing and Applications* Debasis Giri, Swagatam Das, Juan Manuel Corchado Rodríguez, Debashis De, 2024-12-22 This book gathers selected high-quality research papers presented at the 3rd International Conference on Advanced Computing and Applications (ICACA 2024), held virtually during 23-24 February 2024. The topics covered are advanced communication technologies, IoT-based systems and applications, network security and reliability, virtualization technologies, compressed sensors and multimedia applications, signal image and video processing, machine learning, pattern recognitions, intelligent computing, big data analytics, analytics in bio-computing, AI-driven 6G mobile wireless networks, and autonomous driving.

tropical algebra: Intelligent Systems and Applications Kohei Arai, 2024-07-31 This volume is a collection of meticulously crafted, insightful, and state-of-the-art papers presented at the Intelligent Systems Conference 2024, held in Amsterdam, The Netherlands, on 5-6 September 2024. The conference received an overwhelming response, with a total of 535 submissions. After a rigorous double-blind peer review process, 181 papers were selected for presentation. These papers span a wide range of scientific topics, including Artificial Intelligence, Computer Vision, Robotics, Intelligent Systems, and more. We hope that readers find this volume both interesting and valuable. Furthermore, we expect that the conference and its proceedings will inspire further research and technological advancements in these critical areas of study. Thank you for engaging with this collection of works from the Intelligent Systems Conference 2024. Your interest and support

contribute significantly to the ongoing progress and innovation in the field of intelligent systems.

tropical algebra: Proceedings of the 15th International Conference on Soft Computing and Pattern Recognition (SoCPaR 2023) Anu Bajaj, Ajith Abraham, Oscar Castillo, 2025-04-24
This book presents 57 selected papers focused on Smart Health Care from the 14th International Conference on Soft Computing and Pattern Recognition (SoCPaR 2023) and 14th World Congress on Nature and Biologically Inspired Computing (NaBIC 2023), which was held in 5 different cities namely Olten, Switzerland; Porto, Portugal; Kaunas, Lithuania; Greater Noida, India; Kochi, India and in online mode. SoCPaR – NaBIC 2023 had contributions by authors from 39 countries. This Volume offers a valuable reference guide for all medical doctors, scientists, academicians, researchers, students and practitioners in the field of artificial intelligence and smart health care.

Related to tropical algebra

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Home Design Discussions View popular home design discussionsGet help for your projects, share your finds and show off your Before and After

Back to Home: <http://www.speargroupllc.com>